# THE CRYSTAL STRUCTURE OF BICYCLO [3.3.3]UNDECANE-1,5-DIOL AND THE CONFORMATION OF BICYCLO [3.3.3]UNDECANE (MANXANE).

## P. MURRAY-RUST,\* J. MURRAY-RUST and C. I. F. WATT+ Department of Chemistry, University of Stirling, Stirling, Scotland, FK9 4LA

#### **(Received** *in UK* **31** *October* **1979)**

Abstract -The crystal structure of bicyclo [3.3.3] undecane-1,5-diol has been determined. It is monoclinic, P2,: c.  $a = 12.99(2)$ ,  $b = 14.16(2)$ ,  $c = 12.50(1)$ ,  $\beta = 112.42(2)$ °, with two independent molecules in the asymmetric unit. One of these is disordered, but the other has almost exact  $C_{3\mu}$  symmetry and its conformati and precise molecular geometry agree well with previous calculations by molecular mechanics. The molecul shows considerable angle strain, having bridge angles in the range 116-121

Bicyclo  $[3.3.3]$ undecanc.<sup>1</sup> I, is an intriguing molecule since, although it comprises cyclo-octane rings, inspection of molecular models shows that its possible conformations are not flexible, unlike those of most monocyclic 8-membered rings. One of its conformations II (with  $C_{3h}$  symmetry) is particularly attractive, and its resemblance to the triskelion crest (Fig. 1) of the lsleof Man suggested the trivial name'manxane'forthe parent hydrocarbon.

The conformations of manxane and its derivatives have been studied by dynamic NMR' and by molecular mechanics.<sup>2</sup> The calculations favour II as the most stable conformation, but indicate that even this arrangement is highly strained. Confirmation of the high ground state strain has been provided by experimental measurements of the heat of formation.<sup>3</sup> One structural manifestation of the strain is a flattening of the bridgehead systems, and the calculations showed that conversion of a bridgehead to a trigonal center would result in relief of strain. Enhanced cation and radical reactivity at these sites has been linked to relief of strain.<sup>4</sup>

Both 1-aza<sup>5</sup> and 1,5-diazamanxane<sup>6</sup> have been described. The structure of 1 -azabicyclo [3.3.3]undecane has been determined<sup>7</sup> and provides qualitative confirmation of the molecular mechanics calculations in that the molecule has  $C_3$  symmetry, C-C-C angles increased (up to  $120^{\circ}$  see Table 4) and there is mcasurahlc flattening at the bridgeheads. No structural data IS yet available for the hydrocarbon, and as the nitrogen force field differs from that of carbon, no detailed comparison is possible.

Manxane itself is not a good subject for crystallographic investigation since it is disordered, sublimes readily. and reacts rapidly with atmospheric oxygen. We have therefore prepared a crystalline derivative by oxidising manxanc with oxygen to a mixture of the bridghead peroxides and hydroperoxides and reducing the mixture to manxan-l-01 VI and manxan-1,5-diol VII (Scheme). Thcsc were separated chromatographically and, as the alcohol VI was found to be disordered, the crystal structure of VII was undertaken.

*Crystullo~ruphp of hicydo* [ *3.3.3* ] *undecane-* I *,5-dial*  (YII). Large prismaticcrystals were produced as below

<sup>+</sup>Prcsent address: Department of Chemistry, University of Manchester



### MANXANE

Fig. 1. The crest of the Isle of Man and its relationship to manxane.



and mounted on a glass fibre. No sublimation or decomposition seemed to take place. Weissenberg and precession photography gave the following information:

*Crystal data.*  $C_{11}H_{20}O_2$ ,  $M_r = 184.2$ . Monoclinic, space group  $P2_1/c$ .  $a = 12.99(2)$ ,  $b = 14.16(2)$ .  $c = 12.50(1) \text{Å}; \beta = 112.43(2)$ ;  $U = 2124 \text{Å}^3$ ,  $Z = 8$ . MoK $\bar{\alpha}$  radiation,  $\lambda = 0.7107 \text{ Å}$ ;  $\mu = 0.43 \text{ cm}^{-1}$ .

Data were collected from a crystal about  $0.5 \times 0.3 \times 0.3$  mm<sup>3</sup> on a Hilger-Wattslinear diffractometer for layers h0-101 (2969 reflexions, of which 1421 had  $I \geq 3\sigma(I)$  and 0-6kl (2328 reflexions, of which 1058 had  $I \geq 3\sigma(I)$ ). After layer scales had been calculated and applied, the reflexsions were merged  $(R = 0.053$  on *I*) to give 1762 unique data.

Structure solution by direct methods was carried out with MULTAN<sup>8</sup> and all non-H atoms for two independent molecules were revealed in the E-map with the highest figure of merit (25 of the first 26 peaks being interpretable as atoms). This structure could not be refined below  $R = 0.30$  with isotropic temperature factors and it seemed possible that a false solution had been found. Repeated attempts over several years to find alternatives all gave this single solution. The E-map was re-examined manually and it was then seen that some of the peaks in one molecule (A) were highly

distorted into thin ellipsoids. The original structure was then refined' with anisotropic thermal parameters for the heavy atoms and *R* dropped to 0.159 in a single cycle. H atoms with isotropic temperature factors were placed in geometrically calculated positions throughout  $(C-H = 1.08 A)$  and the refinement (with unit weights and two blocks in the matrix) converged after four more cycles at  $R = 0.0842$  (271 parameters). The atoms in molecule B (which had approximate  $C_{3h}$ symmetry) had normal thermal ellipsoids, but molecule A approximated to  $D_{3h}$  symmetry and the bridge atoms exhibited severe tangential anisotropy, though they were still positive definite. The anisotropy was greatest for the mid-bridge atoms  $(C(3), C(7)$  and  $C(10)$ ).

It is clear that molecule A is suffering from either static or dynamic disorder. On energetic grounds (Discussion) it seemed unlikely that the model produced by refinement was chemically acceptable and disordered arrangements were considered. Disorder might arise from a mixture of different conformers (e.g. with  $C$ , or  $D_3$ , symmetry) in the crystal at the A site, but this was felt to be unlikely since II appears to be the most stable conformer<sup>2</sup> by about 6 kcal mol<sup>-1</sup> Orientational disorder of II seems the most probable since the molecule is globular with no strong directional packing forces. Accordingly site A was represented by two molecules (with fractional occupancies summing to unity) sharing the same local 3-fold axis but oriented in opposite directions (Fig. 2). Since this model could produce singularities in the matrix (e.g.  $C(2')$  and  $C(2'')$ are close together) constrained refinement was used  $(C-C$  in molecule  $A = 1.53(2)$  Å). H atoms (disordered) were placed in calculated positions on molecule A and all disordered atoms were given isotropic temperature factors. The B molecule was treated normally. This



Fig. 2. Schematic view along the approximate 3-fold axis of the initial model used for refinement of disordered molecule A. The molecule had refined to a configuration with 3 approximate mirror planes (dashed lines). Atoms on the 3-fold axis  $(C(1), O(1), C(5)$  and  $O(2)$ ) were given unit occupancy. Each other atom X was replaced by two part atoms  $X'$  and  $X'$ whose occupancies summed to unity. The mid-bridge atoms  $(C(3<sup>'</sup>)$ etc.) were displaced from the mirror plane by an amount estimated from models. The remaining bridge atoms X'. X"  $(C(2')$  etc.) initially both had the same position as X, but by constrained refinement with SHELX (all  $C \cdot C = 1.53(0.02 \text{ Å})$ 

positions off the mirror plane were found.

model (280 parameters and 24 equations of constraint) (Table 4) are based on the anisotropic model. This is not refined to  $R = 0.0950$ ; there were some quite large because the anisotropic model is more likely to be refined to  $R = 0.0950$ ; there were some quite large because the anisotropic model is more likely to be elements in the correlation matrix. Comparison of  $R$  *physically* correct (we argue in the Discussion that a elements in the correlation matrix. Comparison of *R physically* correct (we argue in the Discussion that a factors shows that this disordered model is *statistically* disordered model is preferable on chemical grounds) factors shows that this disordered model is *statistically* disordered model is preferable on chemical grounds) worse than the ordered anisotropic one. For this reason but because it better describes the scattering tables of final parameters (Table 1<sup>†</sup>), bond lengths contribution from molecule A and hence allows better (Table 2). bond angles (Table 3) and torsion angles refinement of molecule B.

but because it better describes the scattering

 $\chi$  $\mathbf{r}$  $\overline{z}$ **CIlAJ 422314) 476214) 7021(S) CClBJ 965514) 6529141 228413) CIZAJ SO>4161 530514) 802416) H12AAl 457516) 3675lLo R438(6J til2AdJ 5435l6J 5822(U) 7647161 C12BJ avu5141 1994(Y) 717315) H12BAJ aObl(4J 21081'0 65Y015)**  HL<sub>2</sub>BB) **91uol4J 247214) 7910(S)**  C13AJ **59~418J YdBO(>J nr3117,**  H13AAl **6626181 538513) YO!J717)**  H13AB) **5686(B) 4947lDJ 964917)**  C138) **896215J UY93OJ 7636151**  H!38A, **9818l'jJ SVL515J 053213)**  Hk3Mtl) **8303(S) U912l~J 7Yc'2(5J**  ClYAb **6541l7J 400514J VlY216J**  Ht'tAA) **7331lIJ 4147141 911116)**  HIVAtll **67UOlIJ 58641'+1 lOUY416J 0664141**  CI481 **10023151 862915)**  HI4BA) **10178l51 1167(U) ~536fSJ**  H<sub>t4</sub>B<sub>B</sub>) **984815) -001614J 8aY6(5)**  CtSA) **6llJ4l4J**  3088(\*) **9>44lSJ**  C\5BJ **11115lS~ ~572('tJ d4Y1(4J**  C16A) **49Y415J 276515J 856316)**  HICAA) **Lk36(>J 501915) 9\*5916J**  Hl6AtlJ **492315) 203613) 932616)**  C<sub>16</sub>B<sub>1</sub> **llmavt5J 145514) 8781151 H16BA) 1243015) 1424lUJ u54115J**  H(6BtlJ **12354(S) 142714) 9111(5)**  ct7iij **3973(7J 319lldJ 7dY2114J**  H17AAJ **3515171 508216) 8'+45ll'+J**  ti17AB) **3677t7) 27lltdJ 7172114)**  Cl781 **112YBl5) 24271'4) d52015)**  HI7BA) **1194515) 294514J Ryb415J**  HI7BB) **10666lS) 2436(Y) dYOV(SJ**  CIBA) **3540(b) 4042lYJ 73b616)**  HttlAAJ **28bbtb) 388114J 659716)**  H\tlAtiJ **3238l5J 441814) 7y10161**  CC.SBJ **1072014J 2777(j) 72Y315J**  HI8BA) **105J614J 352713) 75~41s)**  HlBdt)J **1132Ol'o 272813) 688715)**  CtVAJ **'~7U2tSJ 6187tE.J 438415)**  HIVAAJ **491815J 5016151 586315)**  HLYABJ **4026151 40671,) 552115J**  C<sub>(98)</sub> **9837151 149614J 5785(Y)**  HtVBAJ **98tlOlSJ 184214) 503214) HcVtldJ 913715J 1050141 5562(4J CilOA) 55YO1121 3738110) 645217) HIlAA) 53321121 3308llUJ 570717) HIlAt)l 6274ll2J 4203flUJ 646217) CllOts) 1087015J 087514) 628615) Htlt3A) 1093715) UYR414J 55Y115J HllhIM) 1159215) 135914) 663415) 734416) CtllAJ 616715) 3OFl415J**  H15AAJ **589915) 240815) 699916J**  H<sub>t</sub>SAB) **70>4&5J 3176153 7510161 ClllBJ 1097Ol5J 017614) 725415)**  H15BAJ **10238151 -02361'0 6973151 H**(586) **11697155) -025214) 7389151 OllA) 34JOl3J 550413) 63Y614) 0118) 902915) 5Ol4l~J 572413) 012AJ 690813) 238613) 922014) 0128) 1177Ol4J -0134(J) 927414)** 

Table 1. Fractional atomic coordinates  $(x 10<sup>4</sup>)$  with c.s.d.s. in brackets

**tTables of structure factors have been deposited.** 





### $EXPERIMENTIAL$

**1.515(8J** (a) *Preparation of 1,Sdihydroxybicyclo [ 3.3.3* ] *undecane* 

**1.517(9)** *Oxidation of* bicycle [3.3.3]undecane. **Dry 0, was** bubbled **1.501~10J** through **a soln** of **bicycle** [3.3.3]undecane (0.15 g) in pentane **1:471ts1** (50ml) until all the hydrocarbon was consumed (9 hr glc monitoring). The mixture was then cloudy and gave a strongly positive starch iodide peroxide test. Evaporation of solvent under reduced pressure at 10° gave a white sticky mass which was taken up in dry ether (50 ml). LAH (0.2 g) was added and the mixture was refluxed for I hr. The mixture was then cooled and quenched by the addition of  $Na<sub>2</sub>SO<sub>4</sub>$  aq. The organic layer was decanted, dried  $(Na_2SO_4)$  and evaporated to give a waxy solid (0.12g) which on tic examination (silica eluting with ether) showed the presence of 2 major components.<br>Preparative the on silica yielded 1-hydroxy-Preparative bicycle [3.3.3]undecane as the faster moving component  $(0.047g)$  and 1.5-dihydroxybicyclo [3.3.3] undecane as the slower moving component (0.036 g). Sublimation of the latter and recrystallization from acetonitrile gave crystals m.p. 217–18° (sealed tube), m<sup>+</sup> 184.1469 Calc. for  $C_{11}H_{20}C$ 184.1463. v<sub>max</sub> (KBr disc) 3370, 2920, 1420, 1452, 1420, 1359, 1343. 1270. 1240. 1226. 1181. 1162. 1090. 978, 882. 861. 810 cm<sup>-1</sup>  $\delta$ H (CD<sub>3</sub>OH, 300 MHz) 1.78 (m unresolved).  $\delta$ C<sup>13</sup> (CD,OH) 20MHz 22.47 (t) 40.80 (t), 76.53 (s).

#### **DISCUSSION**

The structure contains two crystallographically independent molecules with two A and two B molecules being linked by a cycle of four  $H$ -bonds (Fig. 3). This results in H-bonded sheets parallel to  $(101)$ . The ring of





#### The crystal structure of Bicyclo[3.3.3]undecane-1.5-diol

				Molecule	
				$(\Lambda)$	(B)
C(8)	$-C(1)$	$-C(2)$	$-C(3)$	62.0	-95.9
C(9)	$-C(1)$	$-C(2)$	$-C(3)$	$-71.2$	36.3
0(1)	$-C(1)$	$-C(2)$	$-C(3)$	175.1	152.3
C(2)	$-C(1)$	$-C(8)$	$-C(7)$	$-74.4$	37.9
C(9)	$-C(1)$	$-C(8)$	$-C(7)$	58.6	$-94.2$
0(1)	$-C(1)$	$-C(8)$	$-C(7)$	174.3	152.0
C(2)	$-C(1)$	$-C(9)$	$-C(10)$	60.8	$-94.9$
C(8)	$-C(1)$	$-C(9)$	$-C(10)$	-72.6	37.2
0(1)	$-C(1)$	$-C(9)$	$-C(10)$	172.1	148.9
C(1)	$-C(2)$	$-C(3)$	$-C(4)$	15.4	68.2
C(2)	$-C(3)$	$-C(4)$	$-C(5)$	$-17.8$	$-66.9$
C(3)	$-C(4)$	$-C(5)$	$-C(6)$	$-58.1$	93.4
C(3)	$-C(4)$	$-C(5)$	$-C(11)$	74.7	$-39.0$
C(3)	$-C(4)$	$-C(5)$	$-0(2)$	$-171.8$	$-154.0$
C(4)	$-C(5)$	$-C(6)$	$-C(7)$	75.3	$-38.1$
C(11)	$-C(5)$	$-C(6)$	$-C(7)$	$-56.2$	94.5
0(2)	$-C(5)$	$-C(6)$	$-C(7)$	$-172.0$	$-152.4$
C(4)	$-C(5)$	$-C(11)$	$-C(10)$	$-61.3$	95.0
C(6)	$-C(5)$	$-C(11)$	$-C(10)$	71.3	$-37.8$
0(2)	$-C(5)$	$-C(11)$	$-C(10)$	$-173.3$	$-149.6$
C(5)	$-C(6)$	$-C(7)$	$-C(8)$	$-25.9$	$-68.4$
C(6)	$-C(7)$	$-C(8)$	$-C(1)$	24.0	68.4
C(1)	$-C(9)$	$-C(10)$	$-C(11)$	17.2	69.7
C(9)	$-C(10)$	$-C(11)$	$-C(5)$	$-16.8$	$-68.3$

Table 4. Torsion angles  $(°)$  (e.s.d.'s  $ca. 1$ )

four H-bonded 0 atoms is not planar. and has approximate  $S_4$  symmetry. The angles in the Hbonding scheme are sketched in Fig. 3(b) and suggest that the H one e.g.  $O(2A)$  is aligned towards  $O(1A)$ . There are no short C C contacts which could distort the observed geometries.

Molecule B has near-perfect non-crystallographic  $C_{3h}$  symmetry, (Figs. 4 and 5) in agreement with this being the conformation of lowest energy. The observed bond angles follow the trends observed in III and suggested by force-field calculations for II, and they are compared in Table 5. It can be seen that agreement is good, with perhaps a hint that the force field produces values for  $C-C-C$  angles slightly too large at the bridgehead and too small in the centres of the bridges. However, librational effects may bc important in the crystallographicdata and these will tend to increase the apparent angles in the bridges, so that overall the force field provides a good model for the manxane system. The torsion angles are probably a more stringent test of the usefulness ofthe force field but, unfortunately, these were not published for the calculations. Nevertheless, the general effects discussed by Chang and Schleyer<sup>2a</sup> can be seen clearly in Fig. 5 where the distortions from an unstrained model are shown. A manxane molecule with tetrahedral bond angles can be constructed with no angle strain but there are severe H.. .H repulsions  $[(about 1.3 \text{ Å})]$  between neighbouring bridges. The torsion *angles (cu* 90°) in the bridges are also not optimum. By flattening the bridges somewhat (or

"straightening the knee" in the Manx crest!) the repulsions are lessened and the torsion angles approach 60". In the present X-ray structure (B molecule) the H...H distances between bridges are in the range 1.95 A-2.05 A, very similar to those in of cyclododecane-1,6-diol<sup>10</sup> where the same triangular arrangement occurs. The torsion angles are likewise more favourable (Table4), but this can only be achieved at the expense of some angle strain. By comparing molecules witha bridgedcyclooctaneringwecanseean increasein angle strain with size of bridge. In bicycle [3.3.1 lnonane VIII and its derivatives the conformation is chair-chair and the angles in the bridges are normal (about  $111-112^{\circ}$ ).<sup>11</sup> In the bicyclo [3.3.2] decane derivative  $IX<sup>12</sup>$  however, the cyclooctane ring is boat-chair (as in the present structure) and the bridge angles are  $116 - 117$ °, whilst in the present skeleton (Table 5) they are 120".

Molecule A approximates to  $D_{3h}$  symmetry with nearly planar bridges (Fig. 4). However, Chang and Schleyer<sup>2a</sup> have calculated that this conformation is 45 kcal mol<sup>-1</sup> less stable than that with  $C_{3h}$  symmetry and it is therefore likely that molecule A is disordered in the crystal. The nature of this disorder has not been satisfactorily revealed by the refinement but, since the activation energy for interconversion of enantiomeric  $C_{3h}$  conformers of I is found to be 11 kcal/mol<sup>-1</sup>, it is unlikely that this dynamic process occurs in the crystal. It is probable that since the molecule is globular it can take up different orientations with little difference in



Fig. 3(a). A view perpendicular to (101) of the crystal packing showing the hydrogen-bonded sheets of molecules The intra-sheet hydrogen bonds (shown for one sheet only as dashed lines) form four-membered rings, details ofwhich are given in Fig 3(b). The sheets (one of which is shown in heavy outline with hydrogen bonds) have *pseudo*-tetragonal symmetry and are related by symmetry to give a *pseudo* body-centred arrangement where molecules on one sheet fit into holes in the sheets above and below.



Fig 3(b). The hydrogen bonding scheme. Bond lengths are  $O(2A)-O(1A)$   $(1 - x, y - \frac{1}{2}, 1\frac{1}{2} - z) = 2.761(6)$  Å;  $O(2B)$ O(1A)  $(1 + x, \frac{1}{2} - y, \frac{1}{2} + z) = 2.756(6)$  A; O(2B)-O(1B)  $(2 - x, y - \frac{1}{2}, 1\frac{1}{2} - z) = 2.809(6)$  Å; O(2A)—O(1B) (x,  $- y, \frac{1}{2} + z) = 2.772(6)$  Å.



**Fig. 4. The two independent molecules of bicycle [3.3.3 Jundecane-1.5-diol in the crystal. Molecule B is ordered and has well defined C,, symmetry. Molecule A. though almost certainly disordered, has been refined**  to a configuration with near  $D_{3h}$  symmetry.



**Fig. 5 View down threefold axis ofmanxaneskeleton in (a) Molecularmodel (with tetrahedral carbon atoms). dotted lines. Dihedral angle of"thigh" to "shin" = 96". (b) In the ordered (B) molecule of manxane diol. solid lines. dihedral angle = 121".** 

# **2806 P. MURRAY-RUST et al.**

Table 5. Comparison of bond lengths and angles in bicyclo [3.3.3] undecane systems.

Column (i) represents values observed in the carbon skeleton of VII (this work, B molecule only). Column (*u*) represents **those from the X-ray analysis of 111. Column (iii) represents those calculated by Chang and**  Schleyer.<sup>2a</sup> Column (iv) Average of (i) and (ii).



intermolecular interactions, and that several orientations are present. (This type of disorder is probably also present in the crystals of I and VII).

We would like to dedicate this structure to the memory of the late Professor William Parker who first synthesised and named the manxane system.

#### **REFERENCES**

- <sup>1</sup>M. Doyle, W. Parker, P. A. Gunn, J. Martin and D. D. MacNicol, Tetrahedron Leters 3169 (1970): <sup>8</sup>J. C. Coll, D. R. **Crist. M. C. G. Barrio and N. J. Leonard. J. Am Chem Sot. 94. 7092 (1972).**
- **'"L W. K. Chang, Ph.D. Thesis, Princeton 197O;"J. L. Fry, E. M. Engler and P. v. R. Schleyer, J. Am. Chem. Soc. 95, 8005 (1973):'D. N. J. WhiteandM. Bovill..!. Chem Sot. PerkinII. 1610 (1977).**
- **3W. Parker, W. V. Steele and 1. Watt, J. Chem. Thermudynomics 9, 307** ( **1977).**
- **'"W. Parker. R. L. Tranter,C. I. F. Watt, L. W. K. Changand**  P. v. R. Schleyer, *J. Am. Chem. Soc.* 96, 7121 (1974): <sup>h</sup>G. A.

**Olah,G. Liang, P. v. R. Schleyer, W. Parker and C. 1 F. Watt. Ibid. 99.966 (1977).** 

- **'See Ref.** I (h).
- **'R. W. Alder. R. B. Sessions. J. M Mcllorand M. F. Rauhns.**  *J. Chem. Soc. Chem. Commun. 747 (1977).*
- <sup>7</sup> A. H. Wang, R. J. Missavage, R. S. Byrn and I. C. Paul, *J. Am.* Chem. Soc. 94, 7100 (1972).
- <sup>8</sup>The structure was solved with MULTAN (G. Germain, P Main and M. M. Woolfson, Acta Cryst. A27, 368 (1971): both an earlier version (P. Main, M. M. Woolfson and G. Germain, Univ of York (1971)) and a recent issue (P. Main. **S. E. Hull. 1.. Lessmger. G. Gcrmam. J. I'. Dcclcrcq and M.**  M. Woolfson. MULTAN-78, A System of Computer Programs for the Automatic Solution of Crystal Structures from Diffraction Data, Univs. of York, England and Louvain, Belgium (1978)) gave identical solutions.
- **'All calculations were carried out wtth the SHELX-76 program. G. M. Sheldrick University of Cambridge (1976).**
- **'"0. Ermer and J. D, Dunn?. Chem.** *Comm.* **178 (1971).**  <sup>11</sup>See, for example, J. Murray-Rust, P. Murray-Rust, W. Parker, R. L. Tranter and I. Watt, *J. Chem. Soc. Perkin II*, **149t"( 1979).**
- <sup>12</sup>J. Murray-Rust and P. Murray-Rust. Acta Cryst. B31, 310 **(1975).**